

High Optical Power Cavity with an Internal Sapphire Substrate

—Thermal lensing, thermal compensation &
three modes interactions

Chunnong Zhao

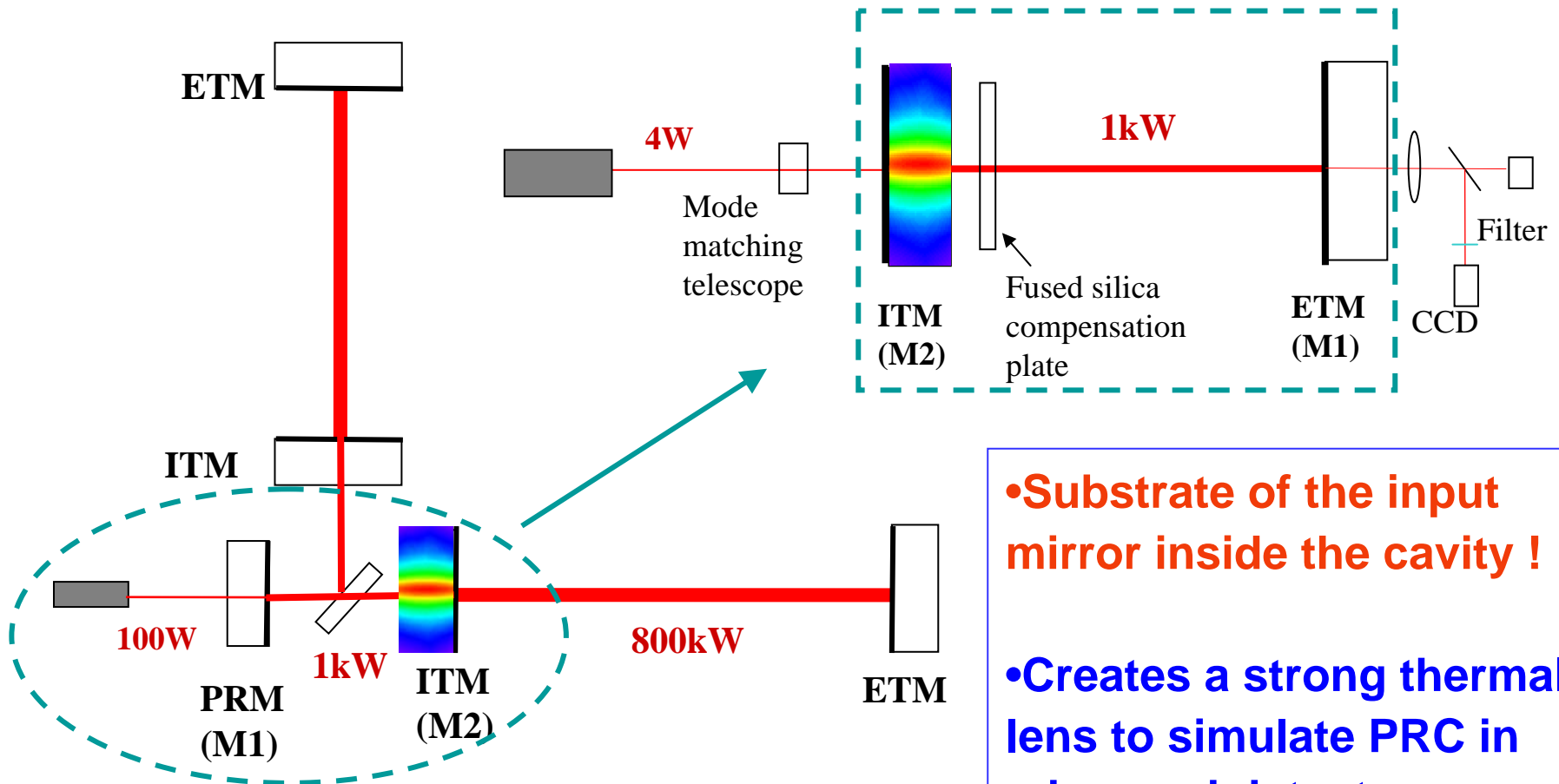
for

ACIGA

Contents

- Strong thermal lensing observation
- Closed loop thermal lensing control
- Observation of beam astigmatism in high power cavity
- Opto-acoustic parametric interactions

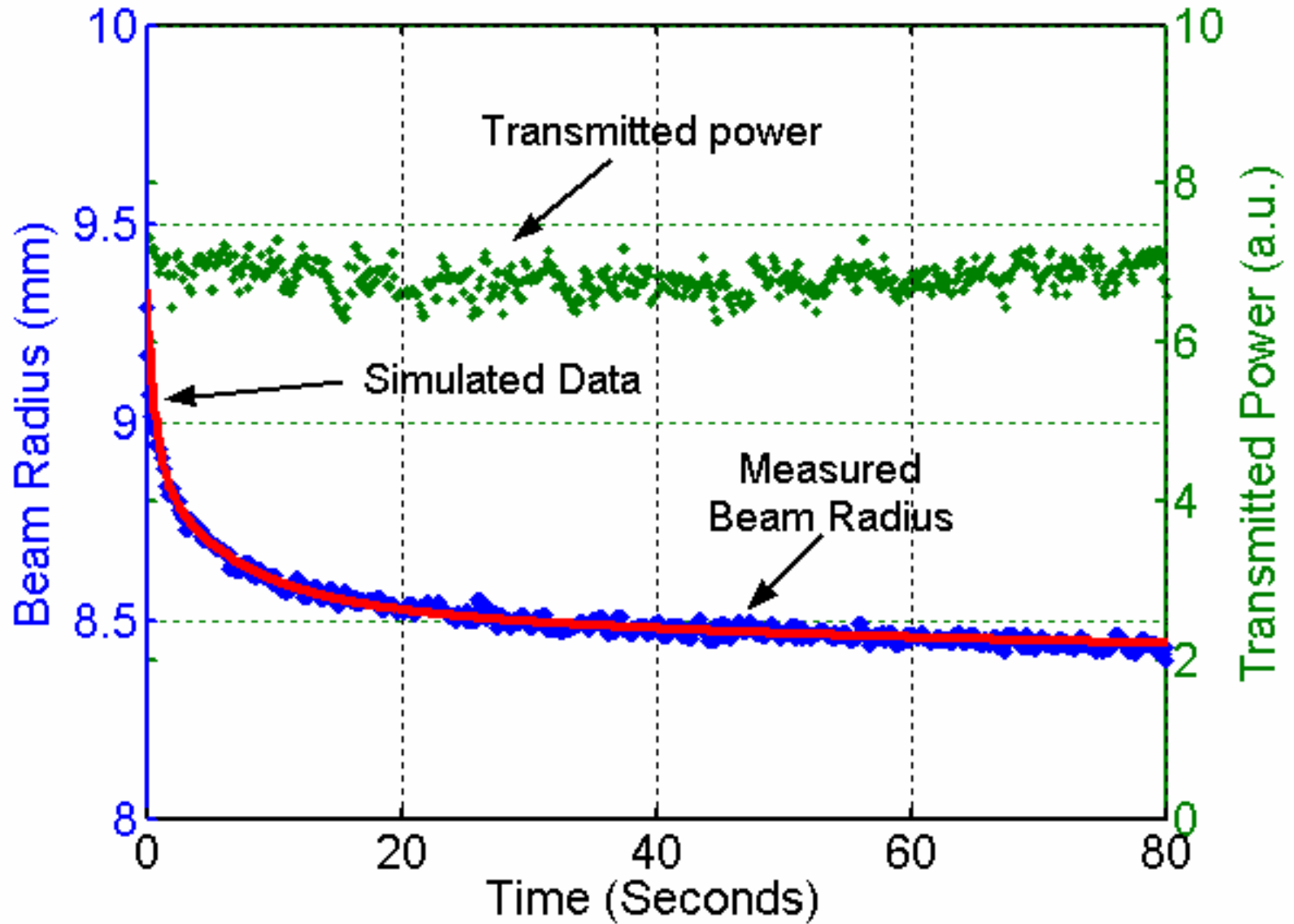
Gingin High Power Facility cavity setup



- Substrate of the input mirror inside the cavity !
- Creates a strong thermal lens to simulate PRC in advanced detectors

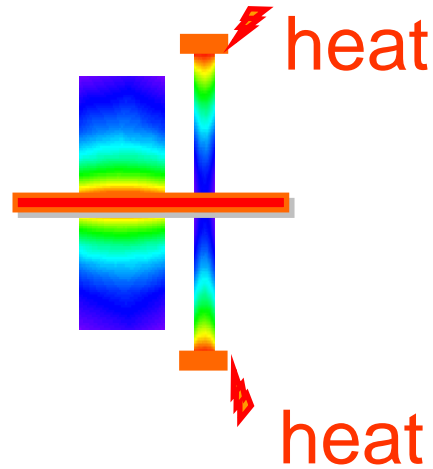
Strong Thermal Lensing

Observation and compensation (PRL 16 June 2006)

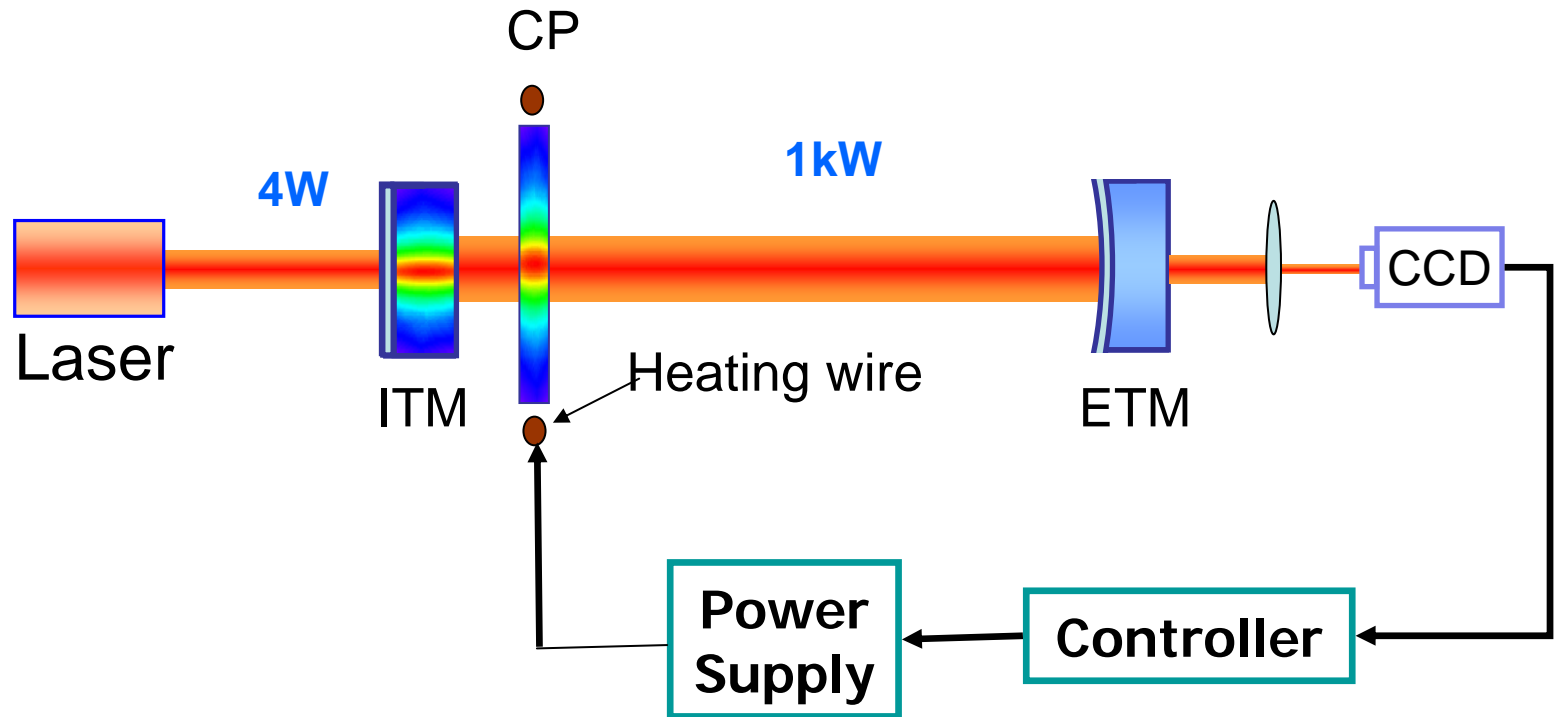


Thermal Lensing and Thermal Compensation

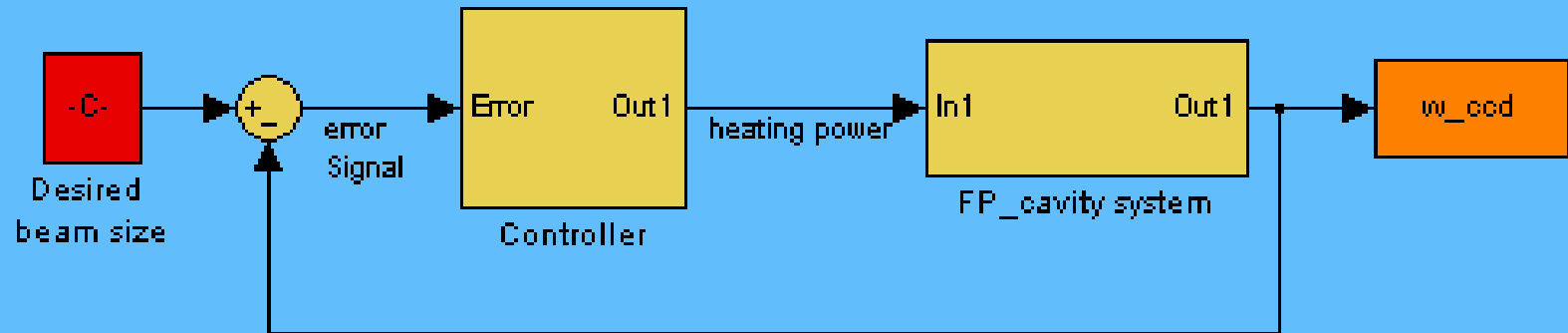
Compensation Plate +
Heating ring



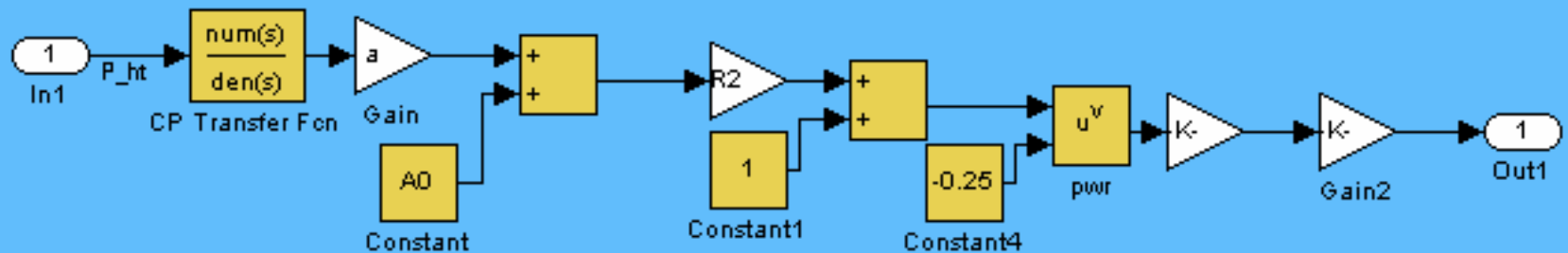
Closed Loop Thermal Lensing Control



Feedback control of thermal lensing compensation

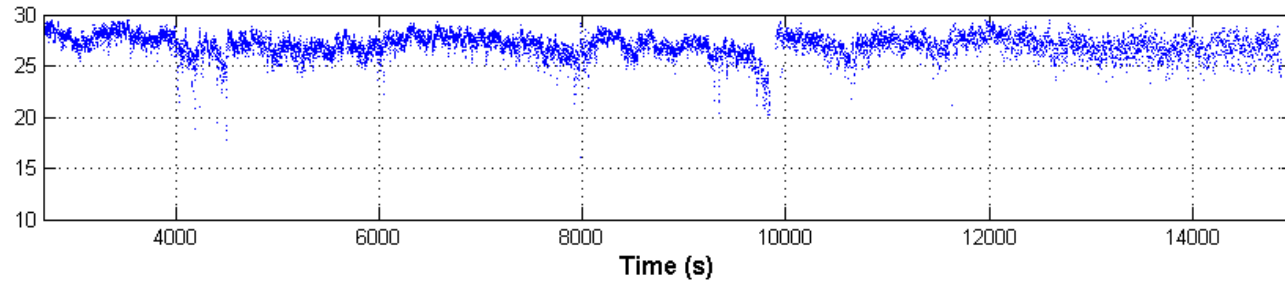


F-P Cavity System

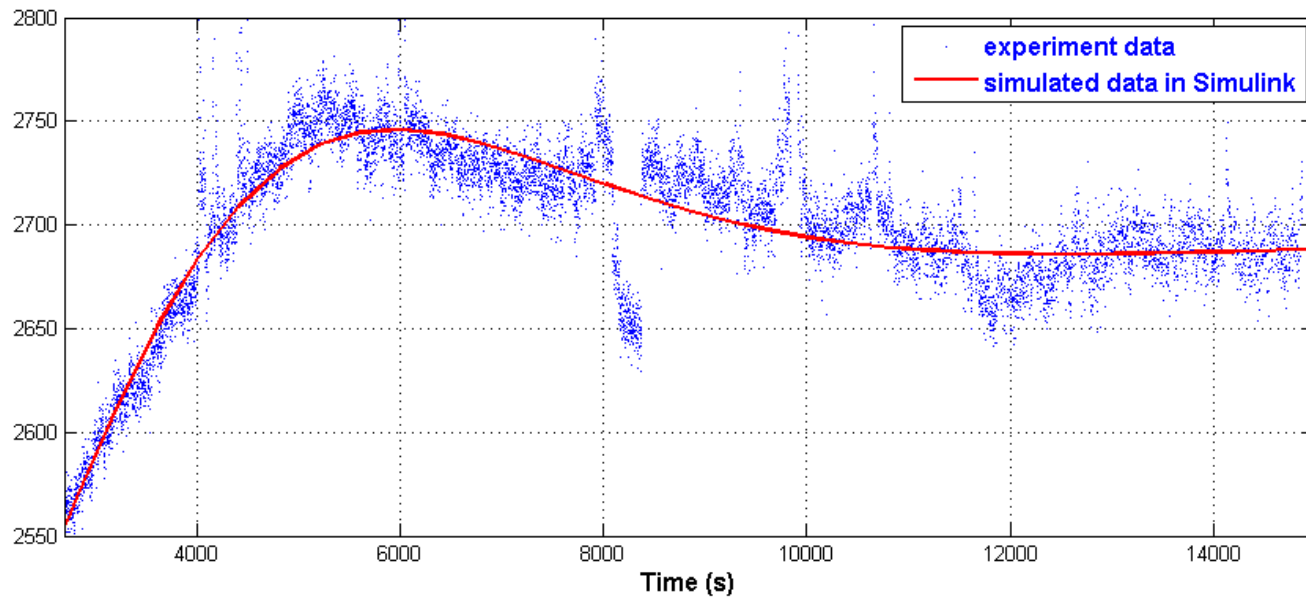


Thermal lensing control Demonstrated

Transmitted Optical Power (a.u.)



Transmitted Beam Size in Diameter (μm)



The beam distortion due to thermal lensing

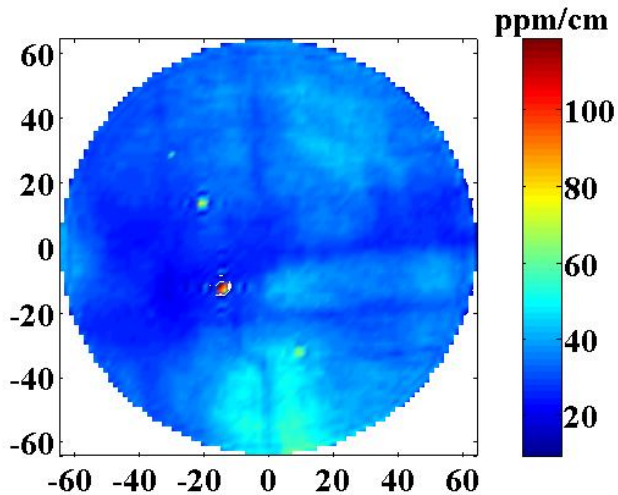
- non-quadratic thermal lensing
- thermal stress birefringence
- inhomogeneous absorption in the test mass

- Sapphire is known to have high inhomogeneity
- Gingin test mass
 - No detailed absorption map
 - At centre ~ 50 ppm/cm (Measured in Caltech, agrees with average thermal lensing measured in Gingin)

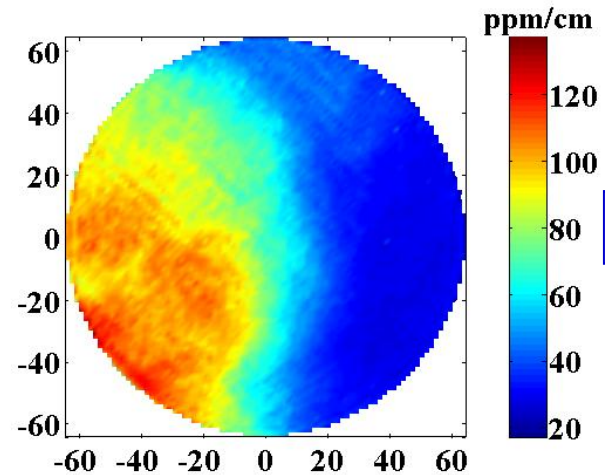
- Analysis of several other samples to get “typical absorption” in sapphire samples

Average absorption across sapphire samples

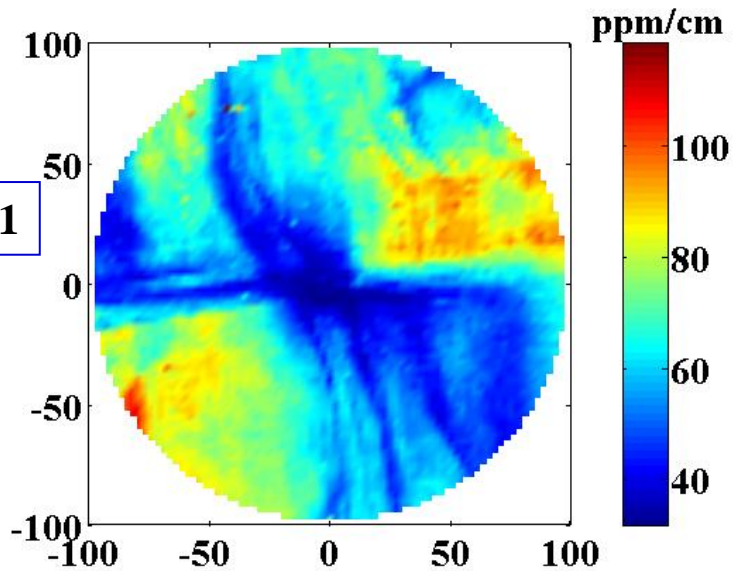
UWA 1



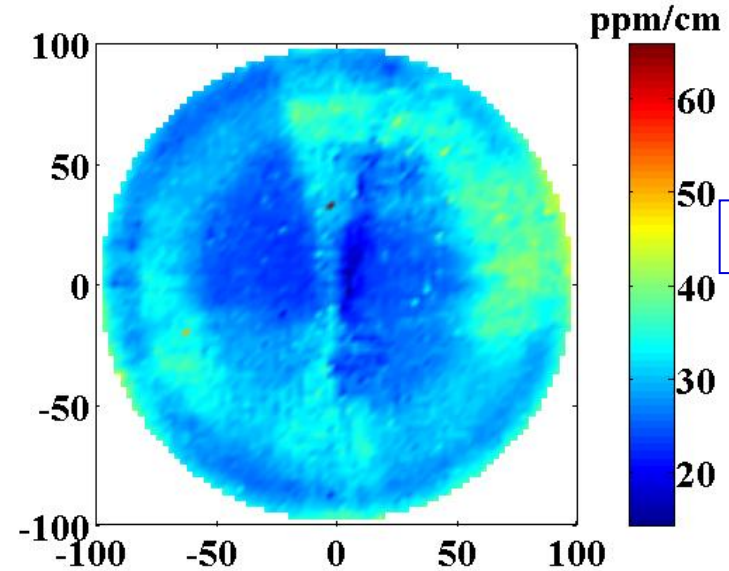
UWA 2



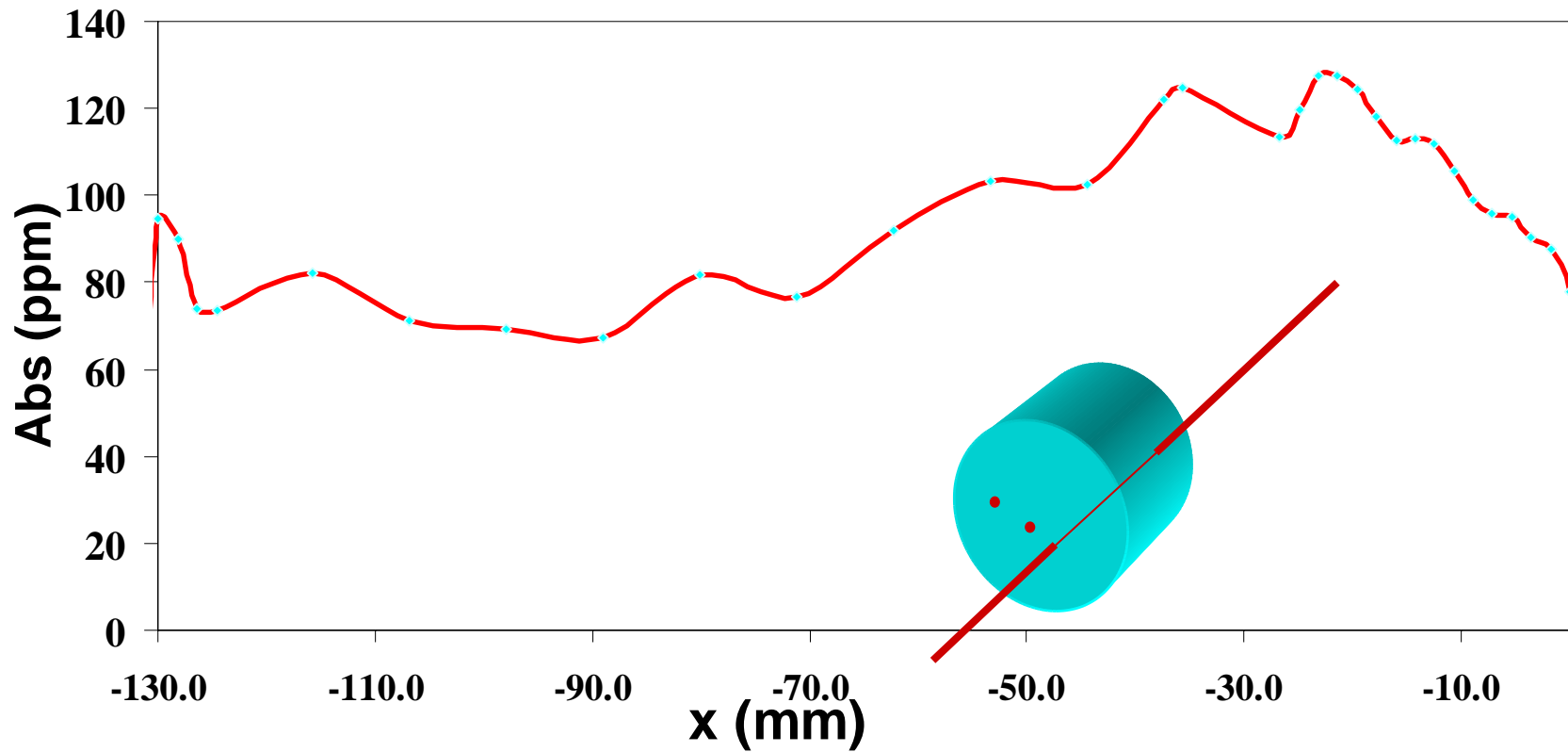
Caltech 1



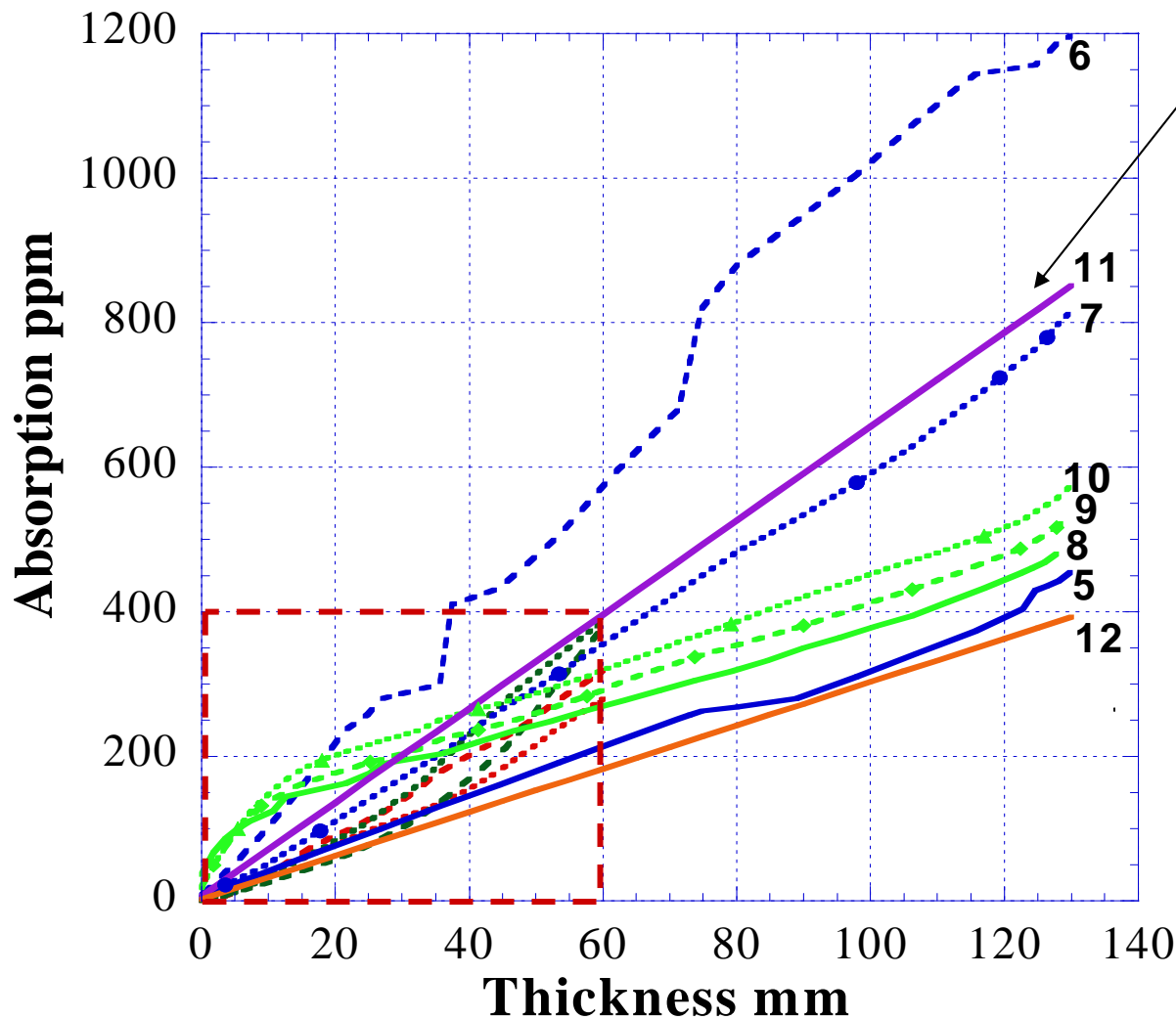
Caltech 2



Example of absorption along the thickness of a sample (Caltech 1)



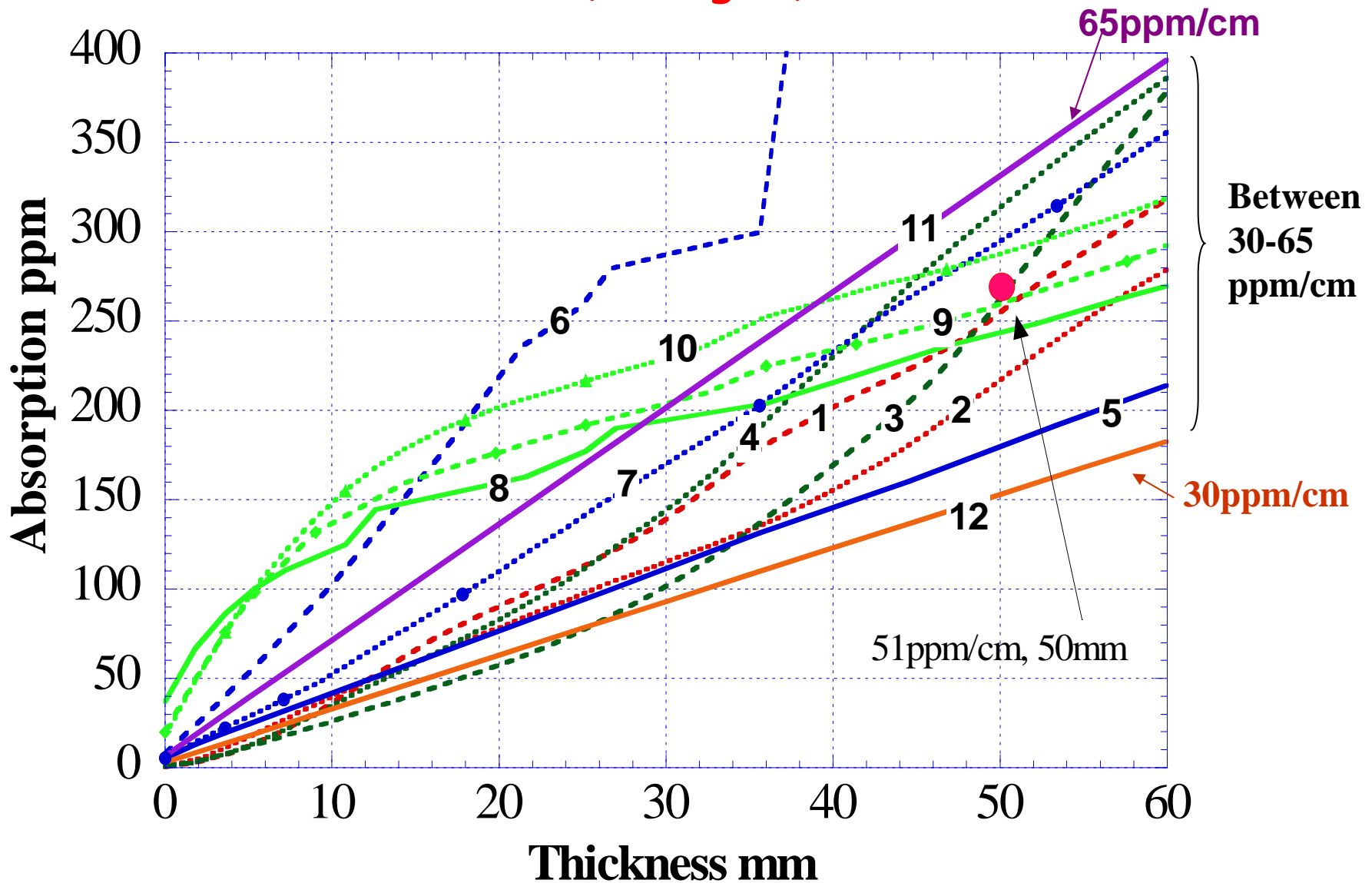
Integrated absorption along the thickness of test masses



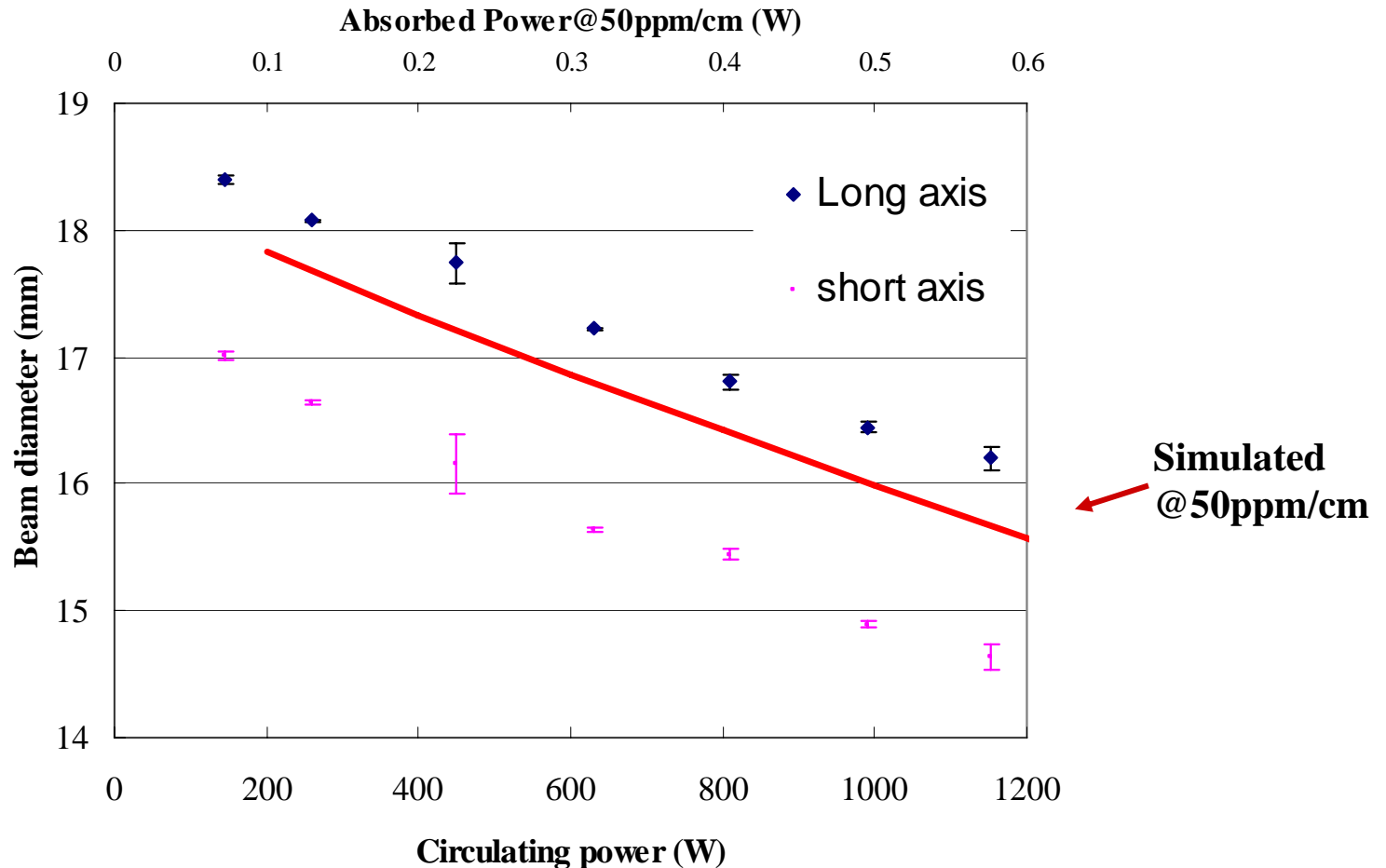
Uniform absorption—
 $\int A(x)dx$ vs. *thickness*
Should be a straight line

- 1. UWA1 (at 50mm from centre)
- 2. UWA2 (at -50mm from centre)
- 3. UWA2 (at 50mm)
- 4. UWA2 (at -50mm)
- 5. Caltech1(at centre)
- 6. Caltech1 (at 50mm)
- 7. Caltech1 (at -50mm)
- 8. Caltech2 (at centr)
- ◇----- 9. Caltech2 (at 50mm)
- ▲----- 10. Caltech2 (at -50mm)
- 11. 65ppm/cm (uniform)
- 12. 30 ppm/cm (uniform)

Integrated absorption along the thickness of test masses (enlarged)

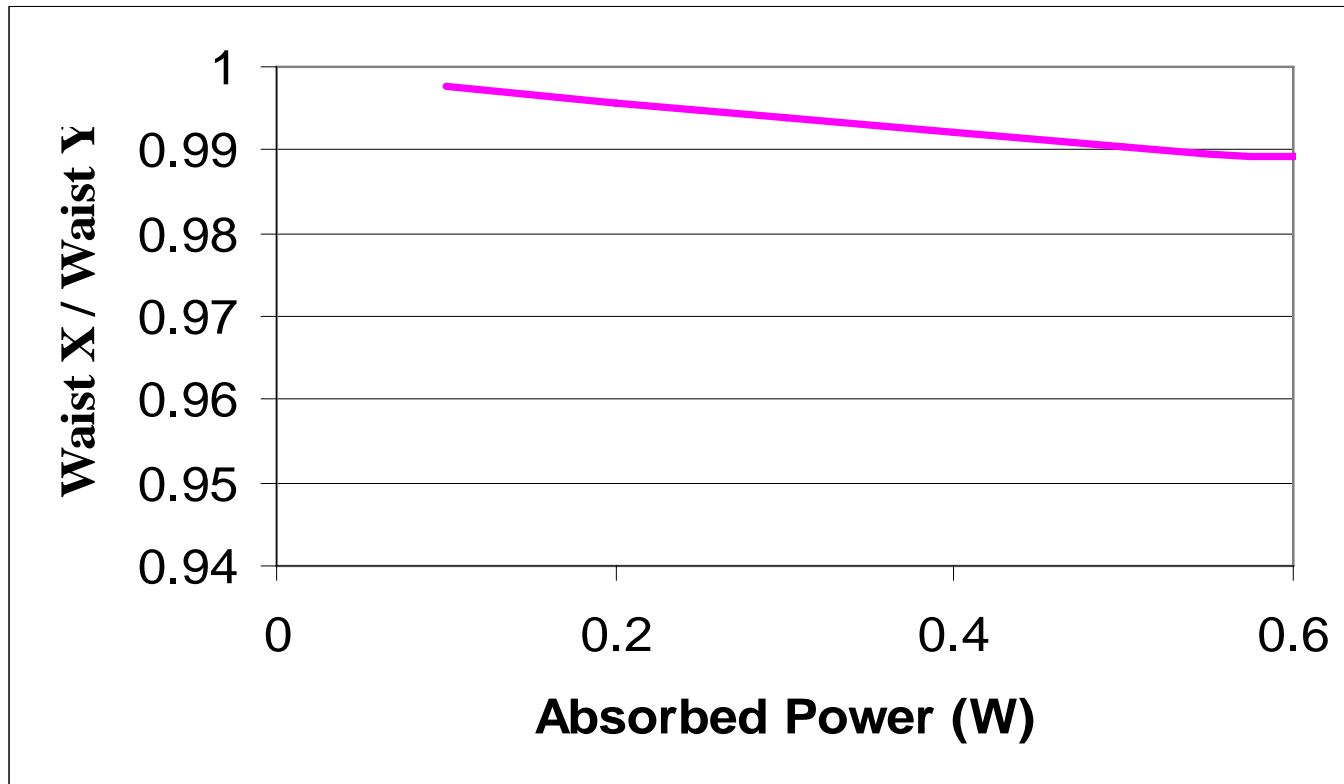


Beam size vs circulating power at Gingin HOPF



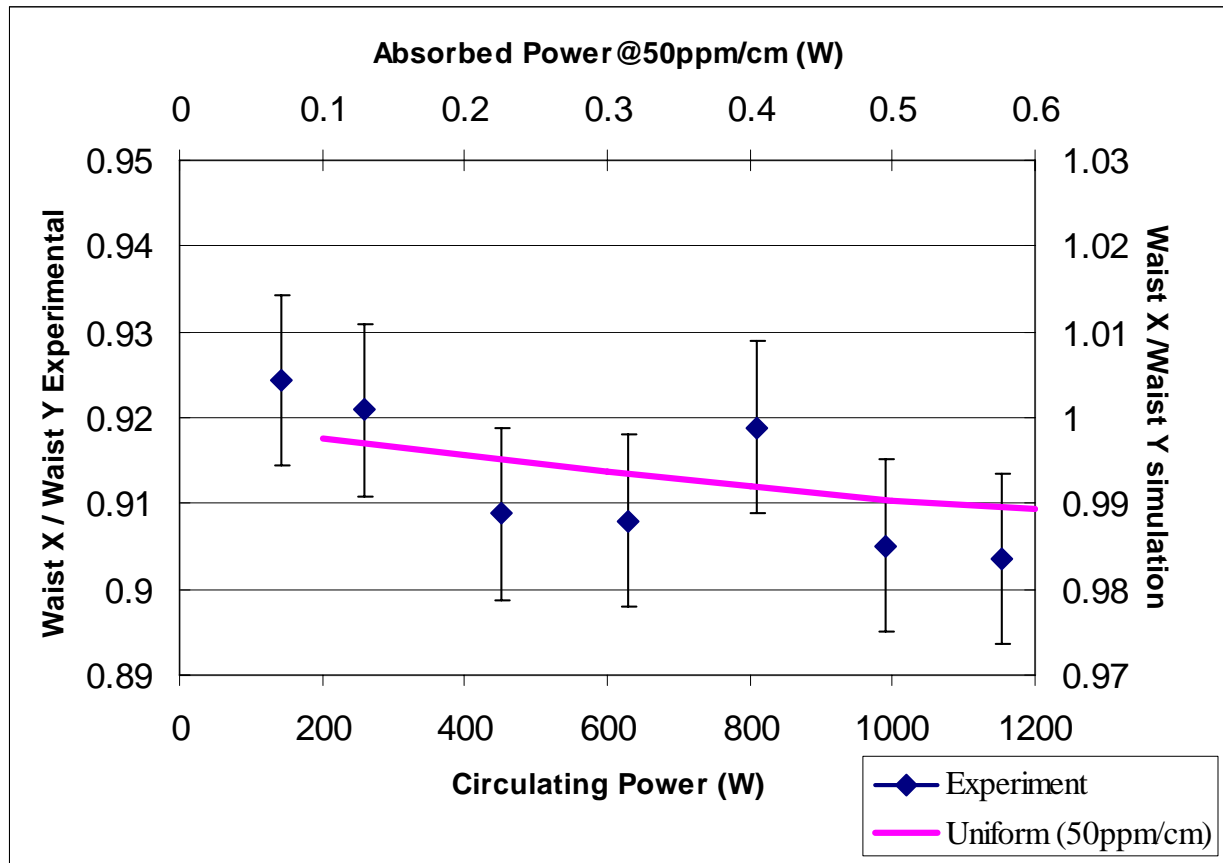
Astigmatism due to birefringence

(simulated sapphire with uniform absorption)



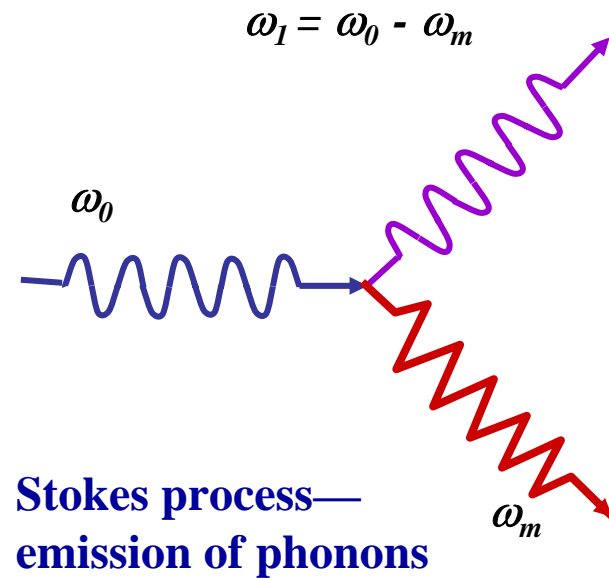
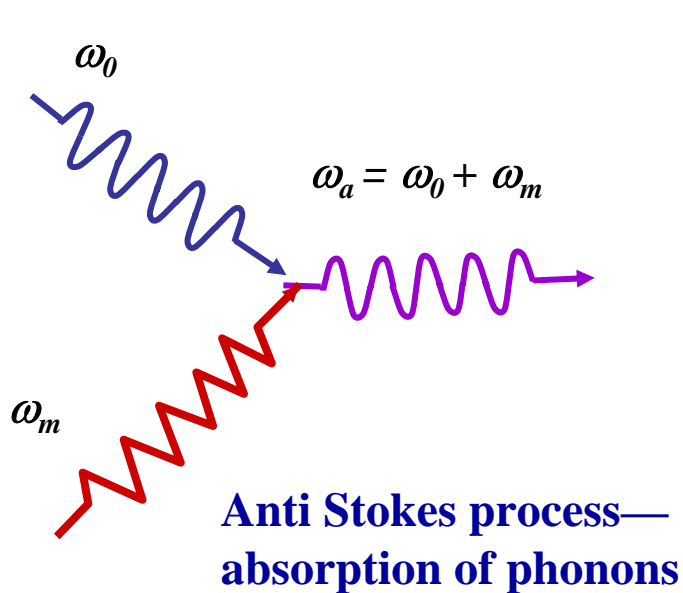
Uniform absorption will still result in power dependent astigmatism due to stress birefringence

Astigmatism vs Circulating Power



- There is an initial systematic astigmatism
- The power dependent astigmatism did not differ much from that due to uniform absorption

Opto-Acoustic Parametric Oscillation



- Some test mass ultrasonic acoustic modes heated(amplified)
- OAPO gain must be kept below acoustic oscillation threshold
- Significant number of modes likely to be excited above threshold in Advanced interferometers.
- OAPO interaction observed at Gingin.

Instability Condition

Parametric gain^[1]

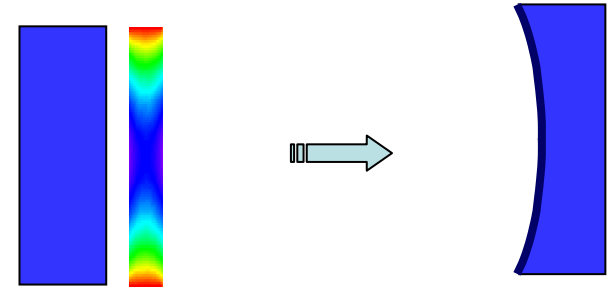
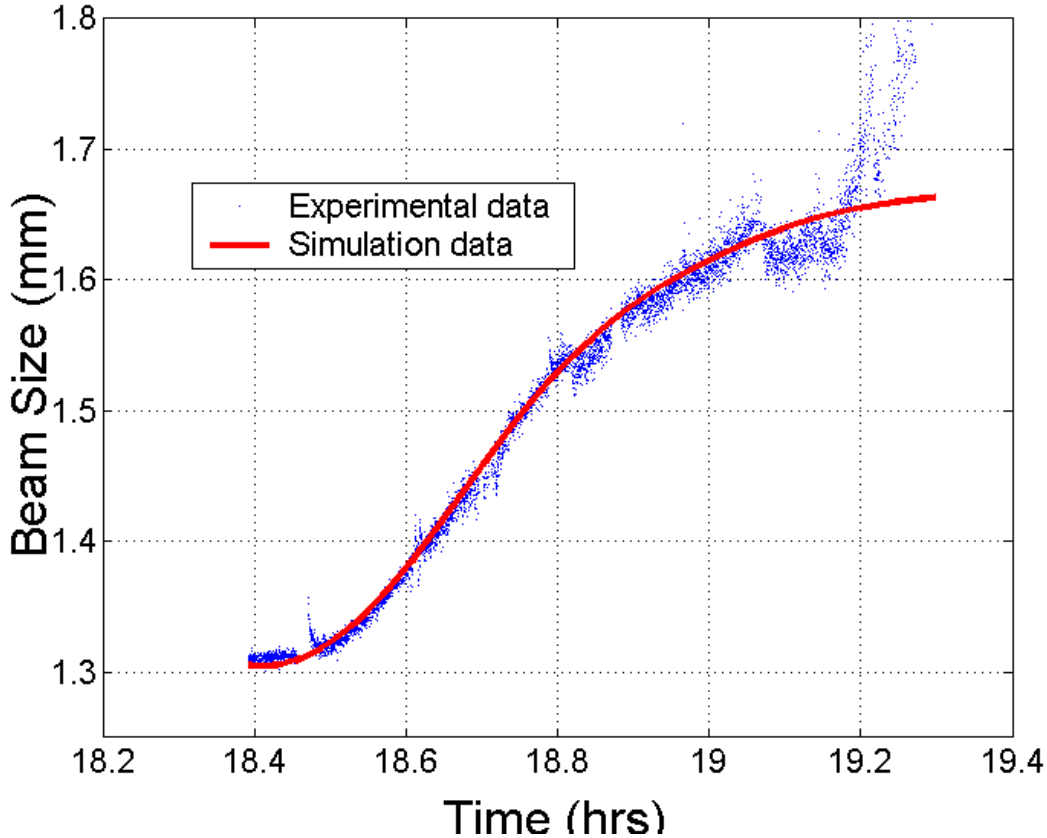
$$R \sim \frac{2PQ_m}{McL\omega_m^2} \left(\frac{Q_1\Lambda_1}{1 + \Delta\omega_1^2 / \delta_1^2} \right) > 1$$

$$\Delta\omega_1 = |\omega_0 - \omega_1| - \omega_m$$

$$\omega_0 - \omega_1 = \frac{\pi c}{L} \left(k_1 - \frac{m + p \times n}{\pi} \arccos \sqrt{\left(1 - \frac{L}{R_1}\right) \left(1 - \frac{L}{R_2}\right)} \right)$$

Changing mirror radius of curvature will change the cavity mode gap

Demonstration of thermal tuning of high order optical frequencies

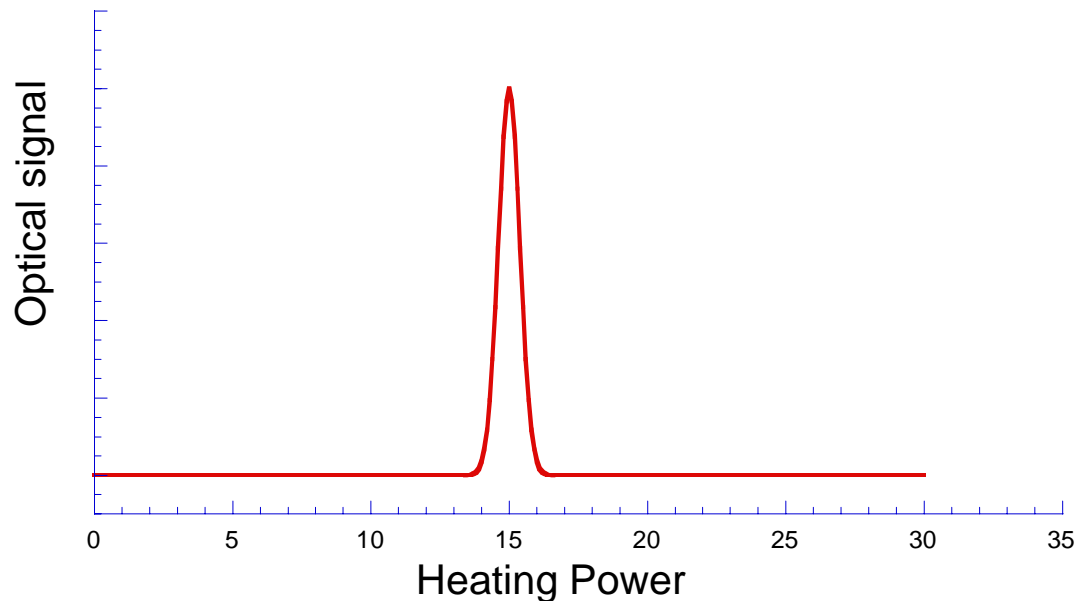


- Heat the compensation plate
- Change the equivalent RoC
- Change the cavity mode spacing

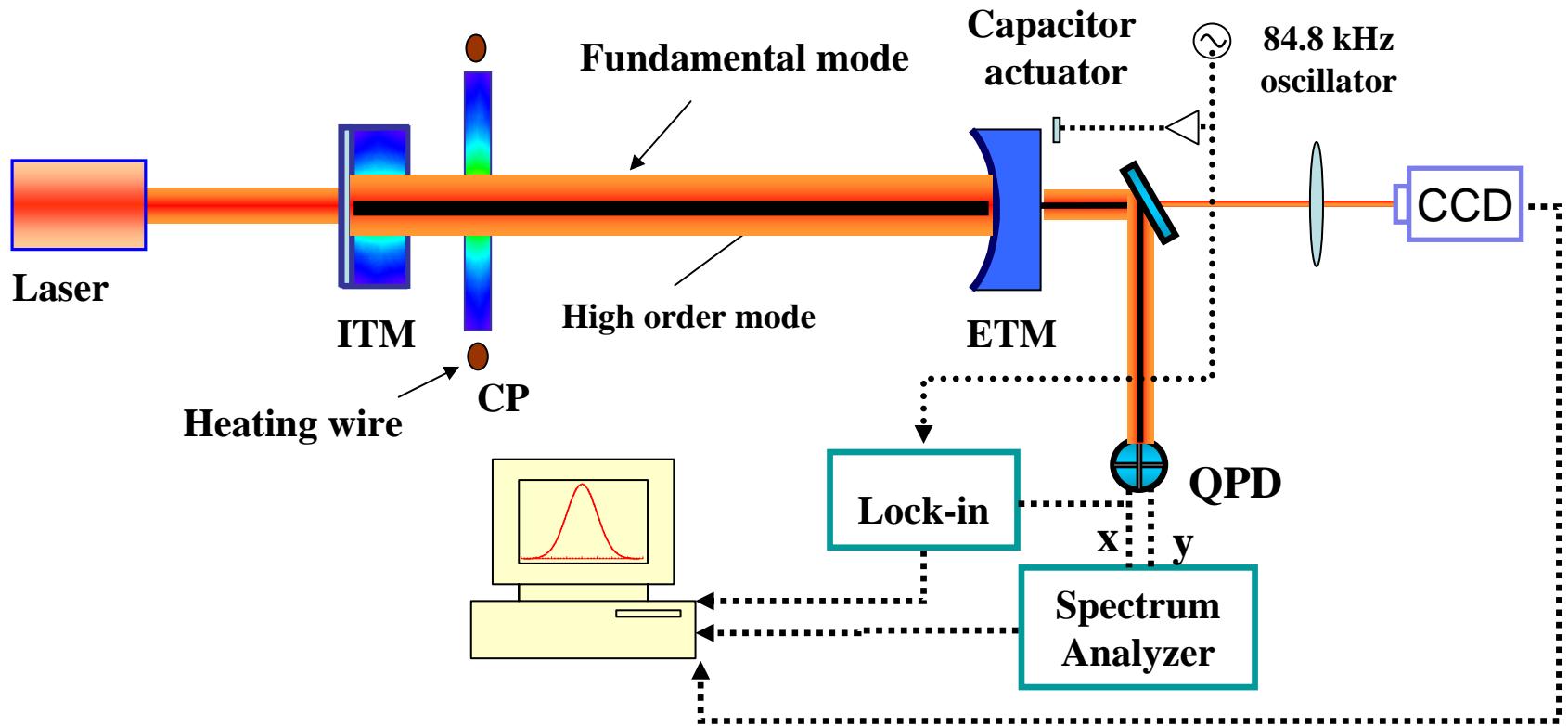
Transmitted beam size  Mode spacing between TEM00 and LG01

Three mode interaction at low power level

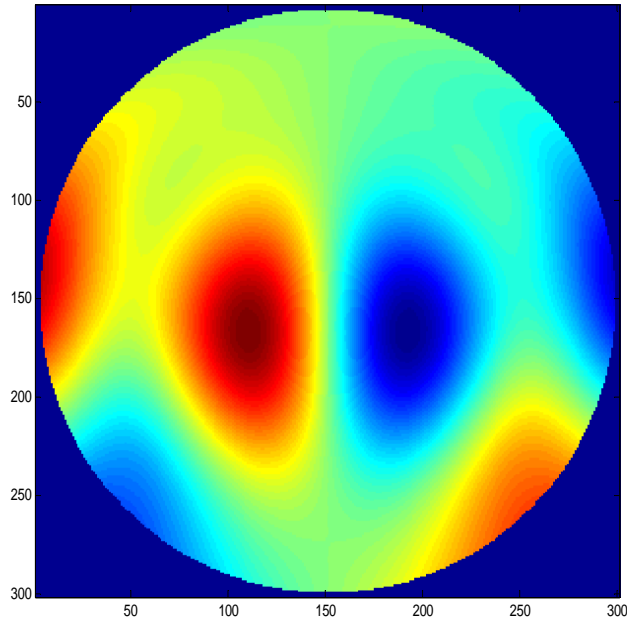
- Excite the target acoustic mode electrostatically
- Observe the high order mode resonance as the HOM resonance frequency is thermally tuned



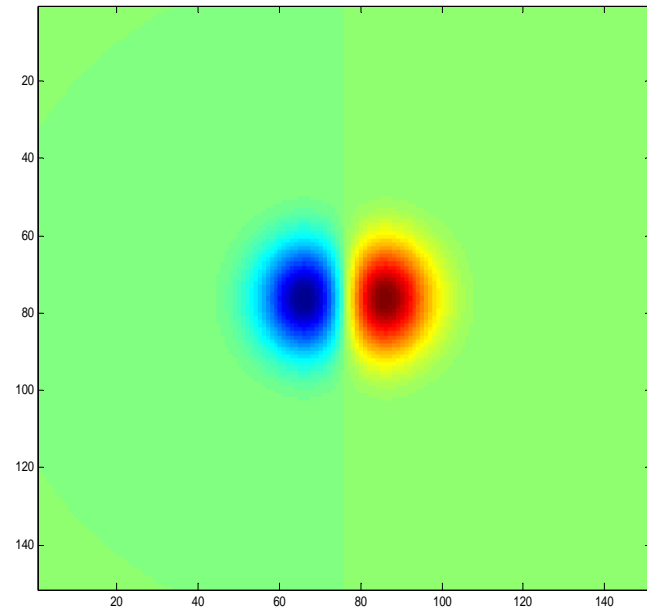
Experimental Setup



Mechanical mode and optical mode overlap

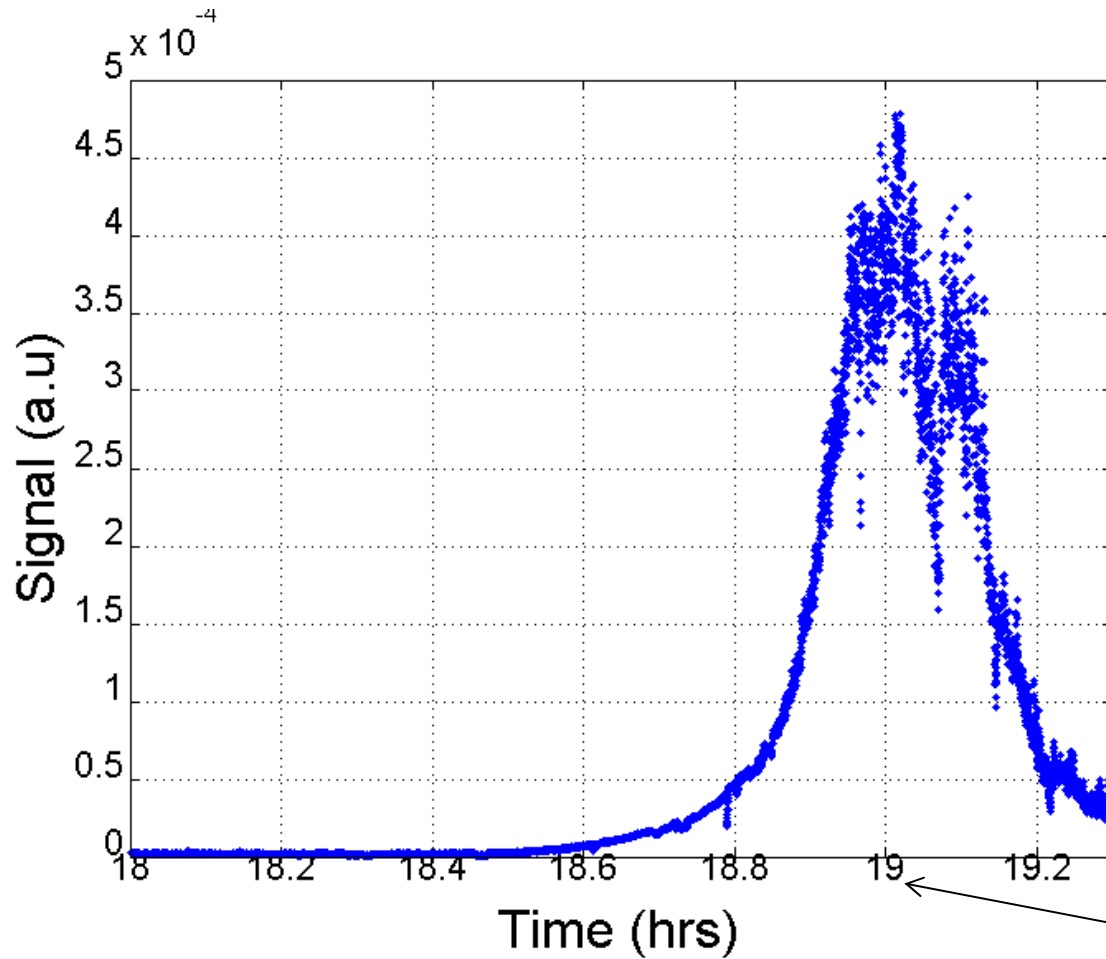


**Mechanical mode
84.8kHz**



Optical mode

Three modes interaction observation at Gingin HOPF



**Amplitude of optical
modes beating signal at
84.8kHz vs. time of
heating (RoC change)**

g factor ~ 0.98

Conclusions

- Feedback control of thermal lensing demonstrated
- Sapphire test mass inhomogeneity effect marginally detectable
- First demonstration of opto-acoustic parametric interactions between the cavity fundamental mode, the cavity high order mode and the test mass acoustic mode (basic physics of parametric instability).

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